

For Poster Report (PR) presentation 2 lectures will be dedicated:

20-th of May, at 13:30, in 509 class.

27-th of May, at 13:30, in 509 class.

During this time you can pass the Mid-Term Exam (MTE) if it is not passed yet.

PR requirements you can find in my Google drive:

https://docs.google.com/document/d/1raqTudLCNlM3wLFCDp_V7QnOg_EFH6d/edit?usp=sharing&oid=111502255533491874828&rtpof=true&sd=true

PR Topics are presented in my Google drive:

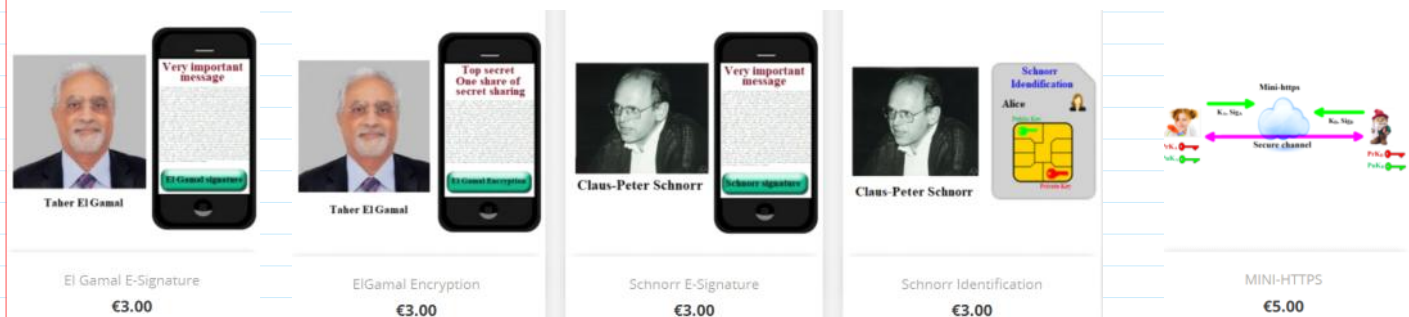
https://docs.google.com/document/d/1B6gavCsgZXcCRssFZEWLvfzaO_IPbC5o/edit?usp=sharing&oid=111502255533491874828&rtpof=true&sd=true

Please select a topic you wish and label this selection in the list.

During the exam you must solve 5 problems from

<https://imimsociety.net/en/14-cryptography>

And oral answer to the 1-2 questions concerning these 5 problems.



Information Confidentiality, Integrity and Authenticity. Person Identification.

Public Parameters $PP = (p, g)$.

$p = 268435019$; $g = 2$;

Information

Encryption/Decryption; Signing/Verification

Person Identification using Zero Knowledge Proof - ZKP

Interactive Zero Knowledge Proof - ZKP

A: ZKP of knowledge x :

$PrK_A = x = \text{randi}(p-1)$

$PuK_A = a = g^x \bmod p$

1. Computes commitment

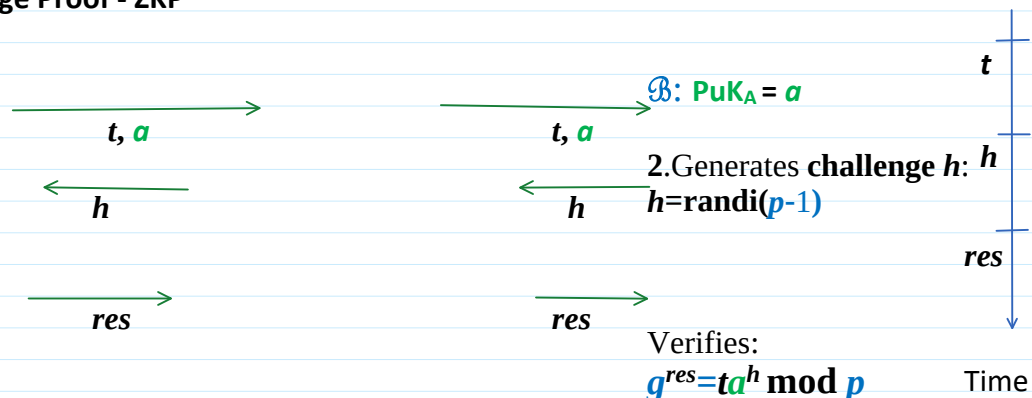
t for random number i :

$i = \text{randi}(p-1)$

$t = g^i \bmod p$

3. Computes response res :

$res = i + xh \bmod (p-1)$



Alice: 'Hello Bob'
 >> M='Hello Bob'
 M; $\sigma=(r,s); a$



$M'; \sigma=(r,s); a$

Bob: let $M'=M$.
 1. Computes $h=H(M||r)$.
 >> $h=\text{concat}(M,r)$
 2. Verifies signature on h .

Non-Interactive Zero Knowledge Proof - NIZKP.

Alice using the scheme of Schnorr Signature can prove a knowledge of any other secret in one or other way related with Discrete Exponent Function - DEF.

Let this secret is some integer i and then Alice using DEF computes so called **Statement** we denote by t for her secret i :

$$t = g^i \text{ mod } p.$$

In this scenario Alice is called a **Prover**.

Then Alice realizes a NIZKP of knowledge of i without revealing i by presenting this **Statement** t to the **Verifier** Bob.

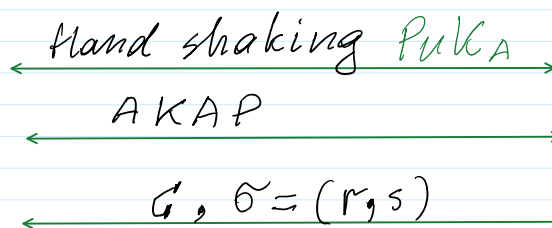
$$\begin{aligned} A: u &\leftarrow \text{randi}(L_{p-1}); \quad L_{p-1} = \{0, 1, 2, \dots, p-2\}; +, -, *, \div \text{ mod } (p-1) \\ r &= g^u \text{ mod } p \\ h &= H(a || t || r) \\ s &= u + i h \text{ mod } (p-1) \\ \sigma &= (r, s) \end{aligned} \quad \xrightarrow{\sigma=(r,s), t, a} \quad \begin{aligned} B: h &= H(a || t || r) \\ g^s &= r \cdot t^h \text{ mod } p \end{aligned}$$

$$g^s = g^{u + i h \text{ mod } (p-1)} \text{ mod } p = g^u \cdot g^{i h} \text{ mod } p = r \cdot (g^i)^h = r \cdot t^h \text{ mod } p$$

Mini-https



$\text{PrK}_A = x = \text{randi}(p-1)$
 $\text{PuK}_A = a = g^x \text{ mod } p$
 k



$\text{PrK}_B = y = \text{randi}(p-1)$
 $\text{PuK}_B = b = g^y \text{ mod } p$

$\text{PuK}_A = a$
 k

$u \leftarrow \text{randi}(p-1)$
 >> $u = \text{int64}(\text{randi}(p-1))$
 $t_A = g^u \text{ mod } p$

1. Verify if PuK_A is in

$u = \text{int64}(\text{randu}(p-1))$

$$t_A = g^u \bmod p$$

$\gg t_A = \text{mod_exp}(g, u, p)$

$$\text{Sign}(x, t_A) = \tilde{\sigma}_A = (r_A, s_A)$$

$i \leftarrow \text{randi}(p-1)$

$$r_A = g^i \bmod p$$

$\gg \text{con} = \text{concat}(t_A, r_A)$

$\gg h_A = \text{hd28}(\text{con})$

$$s_A = (i + x \cdot h_A) \bmod (p-1) = \tilde{\sigma}_A = (r_A, s_A)$$

$t_A, \tilde{\sigma}_A = (r_A, s_A)$
 $\xrightarrow{\text{PuK}_A}$

$t_B, \tilde{\sigma}_B$
 $\xleftarrow{\text{PuK}_B}$

1. Verify if PrK_A is in Data Base.

2. Verify if $\tilde{\sigma}_A$ on t_A is valid.
 $\text{Ver}(\text{PuK}_A, \tilde{\sigma}_A, k_A) = \text{True}$

3. Generates $v \leftarrow \text{randi}(p-1)$
 Computes $t_B = g^v \bmod p$.
 $\text{Sign}(y, t_B) = \tilde{\sigma}_B = (r_B, s_B)$

$$k_{AB} = (t_B)^u \bmod p =$$

$$= (g^v)^u \bmod p = g^{vu} \bmod p = k_{AB} = k = k_{BA}$$

$$k_{BA} = (t_A)^v \bmod p =$$

$$= (g^u)^v \bmod p = g^{uv} \bmod p$$

$\mathcal{A}$: creates transaction T_x

$$E(k, T_x) = \mathcal{C}$$

$j \leftarrow \text{randi}$

$$r = g^j \bmod p$$

$$h = H(\mathcal{C} || r)$$

$$s = j + x \cdot h \bmod (p-1)$$

$$\tilde{\sigma} = (r, s)$$

$\mathcal{C}, \tilde{\sigma} = (r, s)$
 $\xrightarrow{\quad}$

1. $\text{Ver}(\text{PuK}_A = a, \tilde{\sigma}, \mathcal{C}) = \{\text{True}, \text{False}\}$

2. $D(k, \mathcal{C}) = T_x$

3. Performs money transf.

After receiving T_x and σ , Bob according to (2.20) computes h

$$h = H(\mathcal{C} || r),$$

and verifies if

$$g^s \bmod p = r a^h \bmod p.$$

V1 V2

Symbolically this verification function we denote by

$$\text{Ver}(a, \sigma, h) = V \in \{\text{True}, \text{False}\} \equiv \{1, 0\}.$$

This function yields **True** if (2.22) is valid if:

$$\text{PuK}_A = a = F(\text{PrK}_A) = g^x \bmod p$$



MINI-HTTPS
€5.00

1. Mentor sends you Public Parameters ($p=268435019$; $g=2$) of 28 bits length.
 Generate public and private keys $\text{PrK}_A=x$ and $\text{PuK}_A=a$.
 Send public key $[a]$ to the Mentor.

$\gg a$

$a = 39794323$

2. Compute random secret number u of 28 bit length and compute session public parameter t_A . Sign t_A with Schnorr signature scheme by computing two signature components $\sigma_A=(r_A, s_A)$. Send $[t_A, r_A, s_A]$ to the Mentor.

109819746,117664796,114109665

% Alice verifies her signature before sending to Mentor

```
>> g_s=mod_exp(g,s,p)
g_s = 254713335
>> a_h=mod_exp(a,h,p)
a_h = 85497572
>> V1=g_s
V1 = 254713335
>> V2=mod(r*a_h,p)
V2 = 254713335
```

3. Mentor sends you (t_B , $PuK_B=32768$, K_B , $t_B=209399419$, $R=101644938$, $S=18011748$). Verify Mentor's signature $\sigma_M=(R,S)$ on t_B . If signature is valid then taking S compute verification parameter $V_1=g^S \bmod p$. Compute common symmetric secret key k and transform k to the hexadecimal form kh of 32 digits length as it is required for AES128 function. Create the string of message variable m ='MMDD' consisting of the month and day of your birth. Encrypt message m using 1 round of AES128 cipher with key kh_{32} by computing ciphertext $C=AES128(m, kh_{32}, 'e')$. **Attention!** Encryption using 1 round is extremely insecure and is used there to speed up the computations and to make sure of its insecurity. Insecurity is seen by comparing plaintext and ciphertext messages in hexadecimal format. They have non-encrypted digits. C should be entered within ''. Send $[V_1, C]$ to the Mentor for decryption.

```
% AES128(in,kh32,NR,fun) Advanced Encryption Standard symmetric cipher with key length of 128 bits
% Encryption is performed for 1 block of length 128 bits or 16 ASCII symbols
%
% in - plaintext/ciphertext of string type: maximum 16 symbols or shorter
%
% kh32 - shared secret key in hexadecimal number of length=32 (128 bits)
% kh32 can be obtained when shared decimal key k is given using commands:
% >> k=int64(randi(2^28))
% k = 160966896
% >> kh32=dec2hex(k,32)
% kh32 = 0000000000000000000000000099828F0
%
% NR - Number of Rounds (e.g. Nr = 10)
% The smaller NR, the lower security of encryption but the speed of encryption is higher
% The least number of NR is 1 and in this case security lack is evident
%
% fun - letter determining either encryption: fun='e' or decryption: fun='d' functions
```

```
>> kh32=dec2hex(k,32)
kh32 = 0000000000000000000000000003C45716
>> m='1012'
m = 1012
```

```
>> u=int64(randi(p))
u = 190442301
>> tA=mod_exp(g,u,p)
tA = 109819746
>>
>> i=int64(randi(p))
i = 236712983
>> r=mod_exp(g,i,p)
r = 117664796
>> con=concat(tA,r)
con = 109819746117664796
>> h=hd28(con)
h = 243151357
>> s=mod(i+x*h,p-1)
s = 114109665
```

```
>> PuKB=int64(32768)
PuKB = 32768
>> tB=int64(209399419)
tB = 209399419
>> R=int64(101644938)
R = 101644938
>> S=int64(18011748)
S = 18011748
>>
>> con=concat(tB,R)
con = 209399419101644938
>> h=hd28(con)
h = 64128805
```

% Alice verifies her signature

```
>> g_S=mod_exp(g,S,p)
g_S = 20703551
>> V1=g_S
V1 = 20703551
V2 = 20703551
```

% Alice computes common

```
% symmetric secret key k
>> k=mod_exp(tB,u,p)
k = 63198998
```

C = 7e38244d7e3874187ee424183dfc730e

20703551,'7e38244d7e3874187ee424183dfc730e'

4. Ok, let be informed that Mentor gets you a price for your birthday. The sum of the price he is sending to you as a ciphertext (**CM=7e38245d7e38d8187e47241865fc730e**). Please decrypt and check it and then encrypt it again with added string 'ok' right after the sum by computing ciphertext **C1**. Send [C1] to the Mentor. **C1** should be entered within ''.

```
'7e3824847e3840187efa24189efc730e'
```

```
>> CM='7e38245d7e38d8187e47241865fc730e'
```

CM = 7e38245d7e38d8187e47241865fc730e

>>

```
>> M=AES128(CM,kh32,NR,'d')
```

Out = 000000000000000000000000000000003935

$$M = 95$$

>>

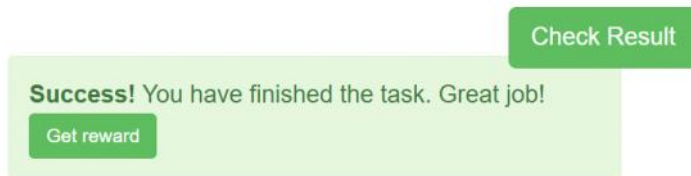
```
>> Mok='95ok'
```

Mok = 95ok

```
>> C1=AES128(Mok,kh32,NR,'e')
```

```
new = ~8$?~8@ ~? ??
```

C1 = 7e3824847e3840187efa24189efc730e



Till this place